



THE UNIVERSITY OF CHICAGO

Department of Statistics

DISSERTATION PRESENTATION AND DEFENSE

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High Dimensional Inference Based on Quadratic Forms

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ABSTRACT

In this talk, we first present a systematic theory for high dimensional analysis of variance in multivariate linear regression, where the dimension and the number of coefficients can both grow with the sample size. We propose a new U type test statistic to test linear hypothesis. Under fairly mild moment conditions, we establish a high dimensional invariance principle, which provides distributional approximation of quadratic forms of non-Gaussian vectors by those of Gaussian ones. Our general framework and theory can be applied to deal with the classical one-way multivariate ANOVA and the nonparametric one-way MANOVA in high dimensions.

We then consider the white noise test for high dimensional time series. Based on a modified Box-Pierce test statistic, we propose a new portmanteau test for detecting serial correlations of high dimensional time series. To obtain the asymptotic distribution of the new test statistic, we develop a new high dimensional Gaussian approximation result for quadratic forms of martingale differences. To estimate the cutoff values, we propose a permutation procedure which avoids estimating the cross-sectional dependencies.