



THE UNIVERSITY OF
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DEPARTMENT OF STATISTICS

PhD Dissertation Proposal Presentation

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“Topics in modern statistical learning: Distribution shift and learning with synthetic data”

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Abstract

his proposal investigates two fundamental challenges in modern statistical learning: (1) learning reliably under distribution shift, and (2) understanding the behavior of AI models trained on recursively generated synthetic data.

(1) Statistical learning under distribution shift: The first part of the proposal develops new non-asymptotic theory for two central problems arising when the training and test distributions differ. We begin with off-policy estimation under adaptive data collection, establishing finite-sample guarantees for a broad class of augmented inverse propensity weighting (AIPW) estimators. These guarantees hinge on a sequentially weighted estimation error of the treatment effect. To control this estimation error, we introduce a general reduction scheme to produce a sequence of estimates that minimizes the sequentially weighted estimation error via online non-parametric regression. Complementary instance-dependent local minimax lower bounds demonstrate the optimality of the proposed methods. We then study covariate shift adaptation, providing structure-agnostic finite-sample learning bounds for doubly-robust (DR) estimators. In parametric settings, we show that DR estimators achieve a fast $O(1/n)$ -rate of convergence of the excess target risk, remarkably independent of the statistical accuracies of the pilot estimates.

(2) Training AI models on synthetic data: The second part of this proposal focuses on model collapse, a phenomenon in which training generative models on their own synthetic outputs leads to progressive performance degradation. Two workflows are typically considered: the discard-workflow, where each generation trains solely on synthetic data from the previous model, and the augment-workflow, which continually accumulates all real data while adding synthetic data

over generations. While the discard-workflow generally induces collapse in parameter estimation, the augment-workflow provably avoids it across linear models, exponential families, and iterative maximum likelihood estimation. This proposal aims to these insights to binary classification. We investigate two key questions: (a) Does the augment-workflow effectively avoid the model collapse for classification tasks? (b) Does the augment-workflow effectively avoid the model collapse? The final part of the proposal presents some theoretical and empirical findings to address these two questions.