



# THE UNIVERSITY OF CHICAGO

## COMPUTATIONAL AND APPLIED MATHEMATICS COLLOQUIUM

---

ANIL DAMLE

Department of Computer Science  
Cornell University

### Uniform Invariant Subspace Perturbation Theory and Applications

THURSDAY, March 12, 2020, at 4:00 PM  
Jones 226, 5747 South Ellis Avenue

#### ABSTRACT

There are many classical results that allow us to understand how invariant subspaces of a matrix behave with respect to perturbations of that matrix. However, they often capture changes in invariant subspaces with respect to the spectral or Frobenius norm whereas many modern applications require control of such perturbations with respect to “row-wise” norms (such as the two-to-infinity matrix norm). These applications include a diverse range of problems such as fitting statistical models and computing localized basis functions in computational quantum chemistry. For example, many algorithms for spectral clustering are either directly motivated by or may be analyzed by understanding properties of invariant subspaces.

In this talk we present new deterministic bounds on how invariant subspaces change with respect to the two-to-infinity norm as a result of perturbations to the underlying matrix. We also argue why aspects of our bounds are tight and show in what settings they improve on other recent results. In particular, understanding in what ways our bounds are tight deterministically makes them an ideal starting point for the analysis of specific algorithms and applications (particularly for random models). To illustrate this point we provide several numerical examples and show how our bounds are useful for a variety of applications.

---

#### Organizer:

Daniel Sanz-Alonso, Department of Statistics, [sanzalonso@uchicago.edu](mailto:sanzalonso@uchicago.edu)  
CAM Colloquium URL: <https://cam.uchicago.edu/events/cam-colloquium/>.

For further information and inquiries about building access for persons with disabilities, please contact Zellencia Harris, [zellenciah@uchicago.edu](mailto:zellenciah@uchicago.edu). If you wish to subscribe to our email list, please visit the following website: [https://lists.uchicago.edu/web/subscribe/cam\\_colloquium/](https://lists.uchicago.edu/web/subscribe/cam_colloquium/).